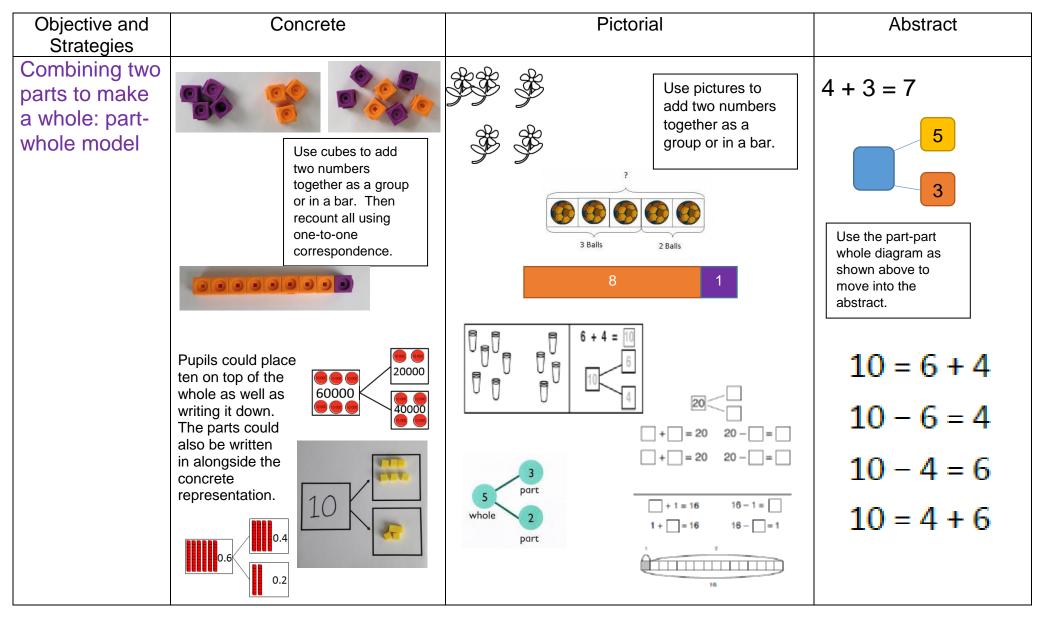
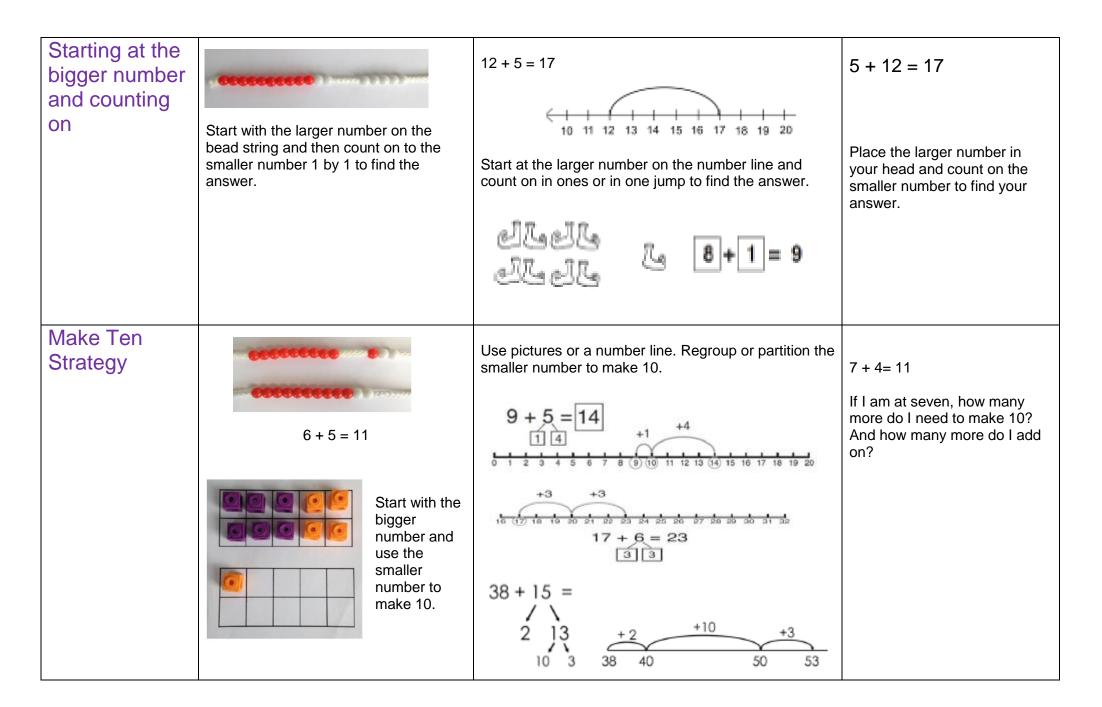
Calculation Policy

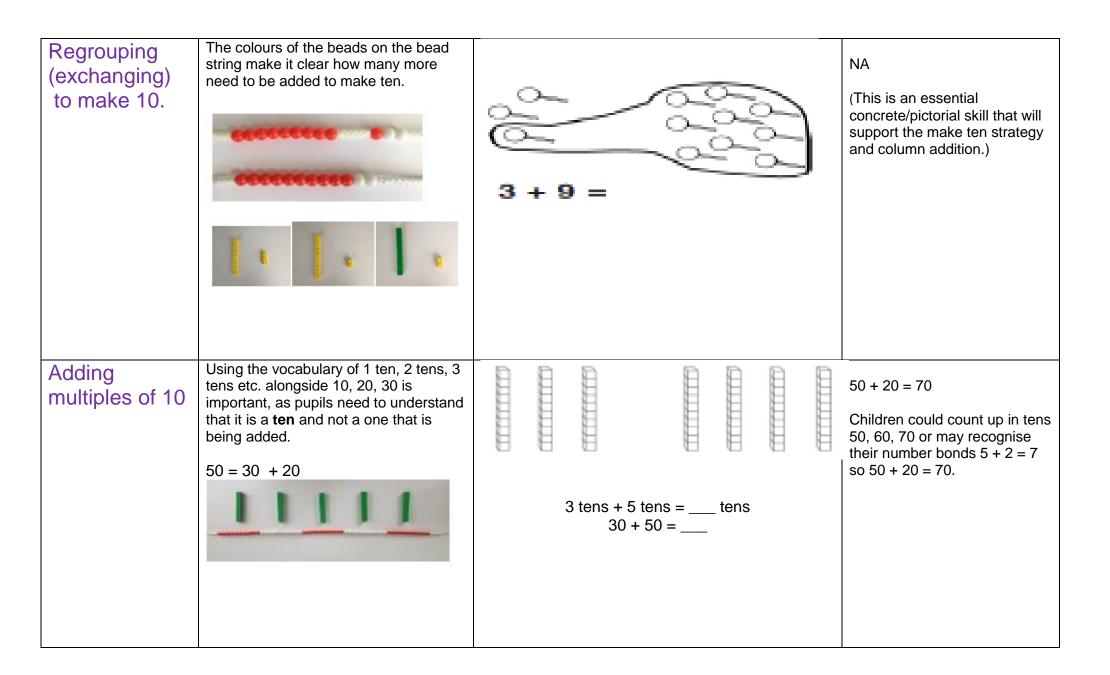


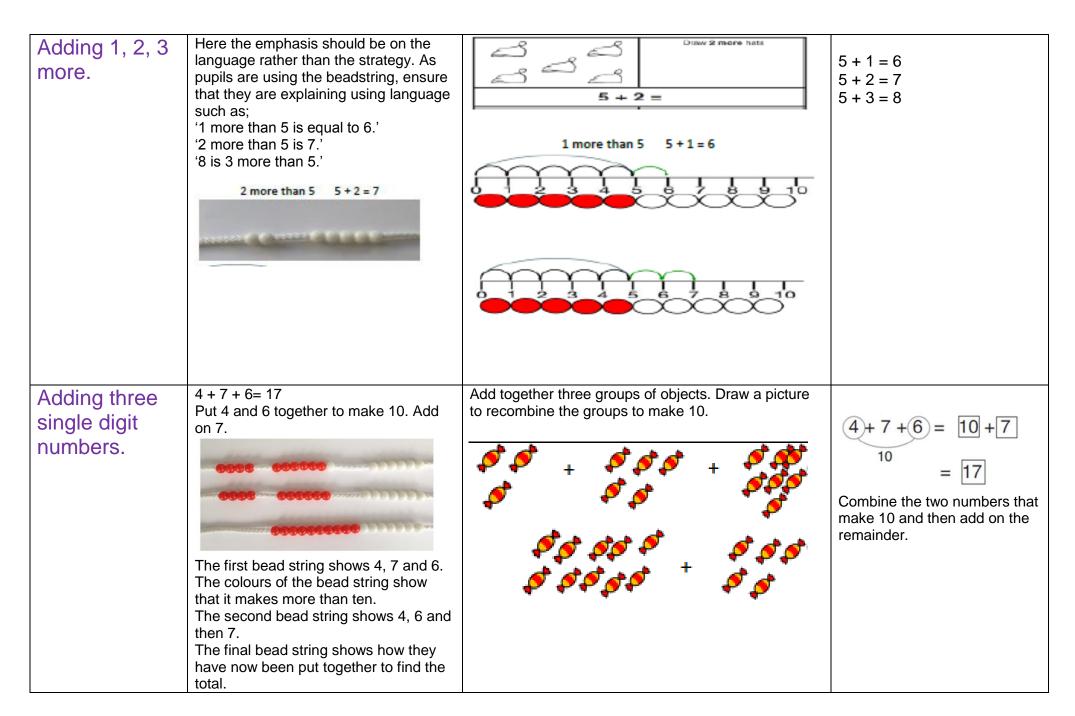
Addition



September 2017. Images and ideas drawn from Mathematics Mastery, White Rose Maths Hubs and various Camden schools' calculation policies.

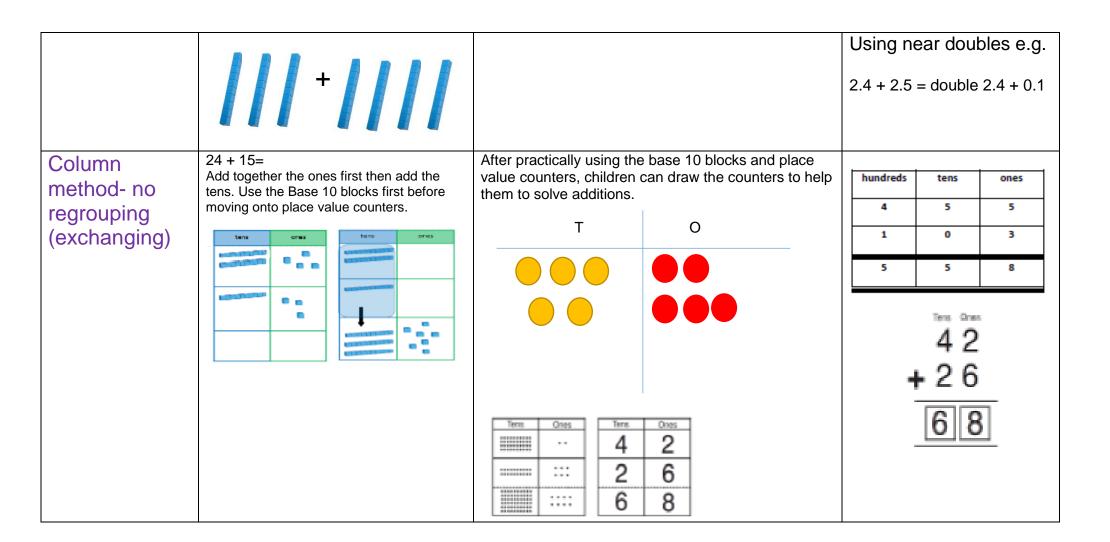




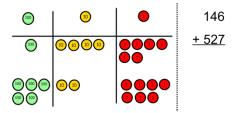


Partitioning one number, then adding tens and ones.	Pupils can choose themselves which of the numbers they wish to partition. Pupils will begin to see when this method is more efficient than adding tens and taking away the extra ones, as shown.	22 32	22 + 17 = 39 Counting up in head: 22, 32, 39.
		22 + 17 = 39	
Partitioning one number then counting 'on'.	Partition with cubes, dienes, bead string, counters, place value counters.	Pupils should be exposed to situations we build an understanding of the fact that character in which the parts are added or surnot change the result. +10 000 +2000 54 623 +77 +300 +12 000 54 623 54 623 54 700 55 000 67 0	nanging the heads e,g,
Using known facts (I know, so)	+		4 = 7 5 X 4 = 20 ds to So 50 x 4 = 200 + 40 = 70 So 50 x 40 = 2000 ds to Etc. 0 + 400 = 700 Reasoning chains can be of great use to encourage children to use their known facts.

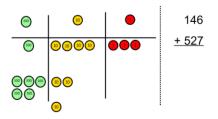
September 2017. Images and ideas drawn from Mathematics Mastery, White Rose Maths Hubs and various Camden schools' calculation policies.



Column methodregrouping (exchanging) Make both numbers on a place value grid.

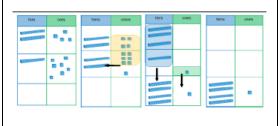


Add up the units and exchange 10 ones for one 10.

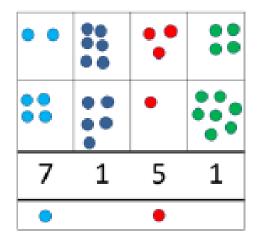


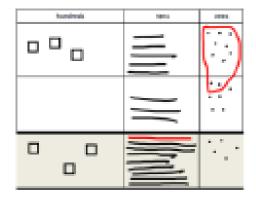
Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

As children move on to decimals, money and decimal place value counters can be used to support learning.



Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.





	hundreds	tens	ones
	3	5	8
+		.3	7
	3	9	5

Start by partitioning the numbers before moving on to clearly show the regrouping below the addition.

$$\begin{array}{rrrr} 20 & + & 5 \\ \underline{40} & + & 8 \\ 60 & + & 13 & = 73 \end{array}$$

As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.

Use a line in between the final addend and the answer for exhanging.

Count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 (including tenths and hundredths – Y6)

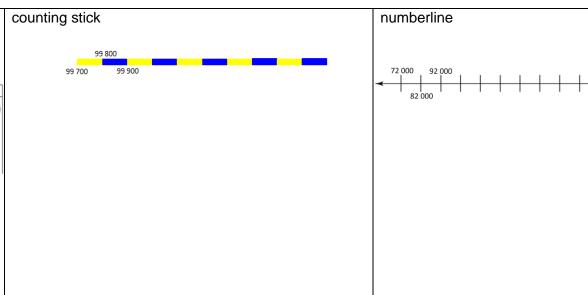
In Year 4, pupils use place value knowledge to mentally add and subtract multiples of 10, 100 and 1000 for numbers up 10 000 In Year 5 this is extended to numbers up to 1 000 000.

In Year 6 this is extended to numbers up to 10 000 000.

Place value grid with counters

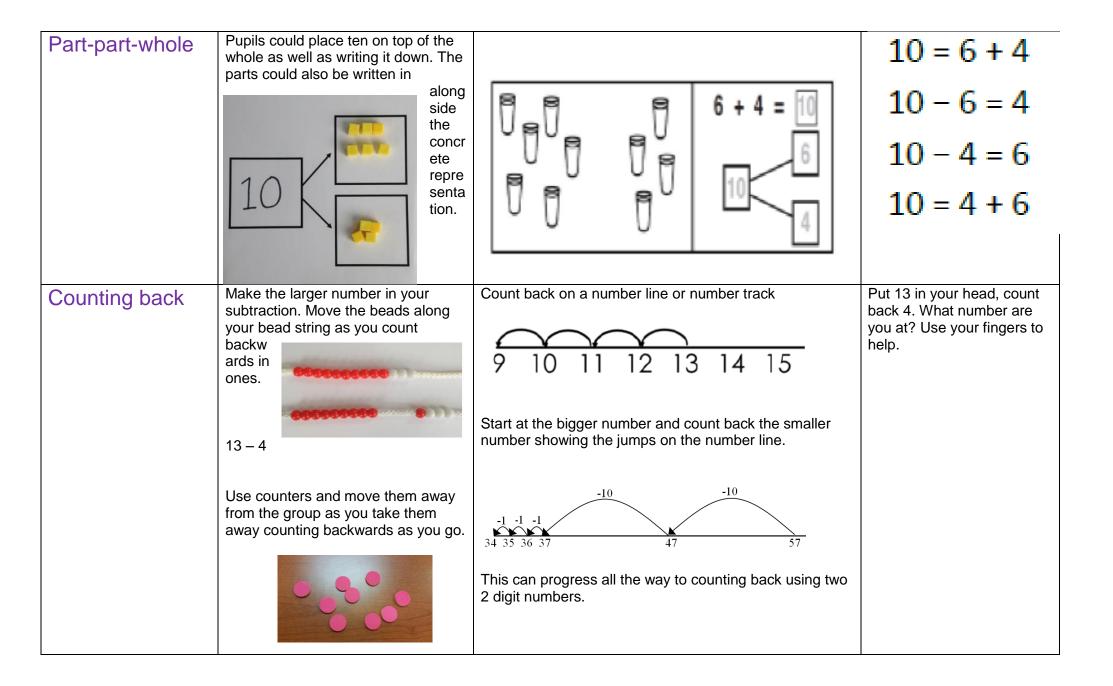


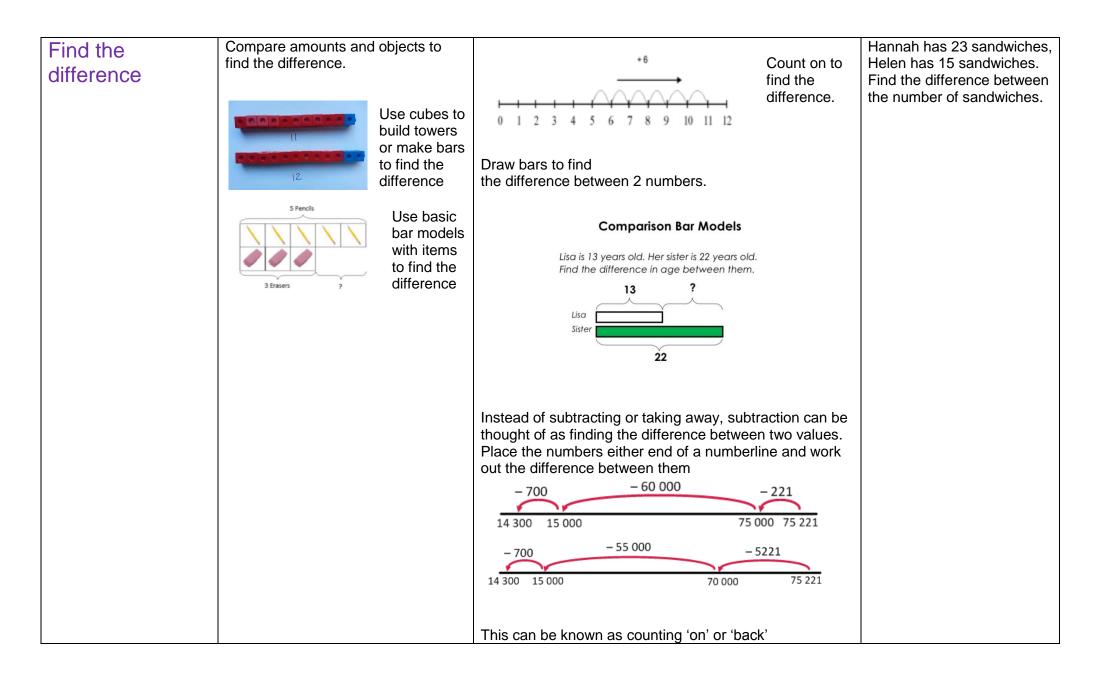
Pay particular attention to boundaries where regrouping happens more than once. E.g. 9900 + 100 = 10000; 99 900 + 100 = 100 000

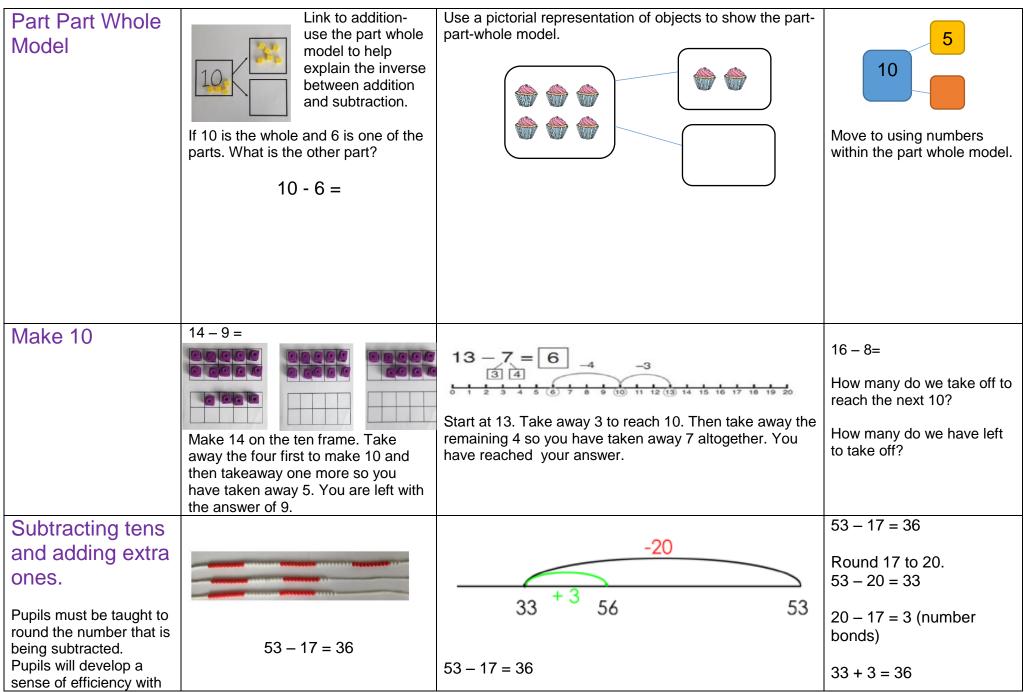


Subtraction

Objective and Strategies	Concrete	Pictorial	Abstract
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away.	Cross out drawn objects to show what has been taken away.	18 -3= 15 8 - 2 = 6
When this is first introduced, the concrete representation should be based upon the diagram. Real objects should be placed on top of the images as one-to-one	$6-2=4$ \longrightarrow	28 - 4 =	0-2=0
correspondence, progressing to representing the group of ten with a tens rod and ones with ones cubes.		$ \begin{array}{cccc} $	





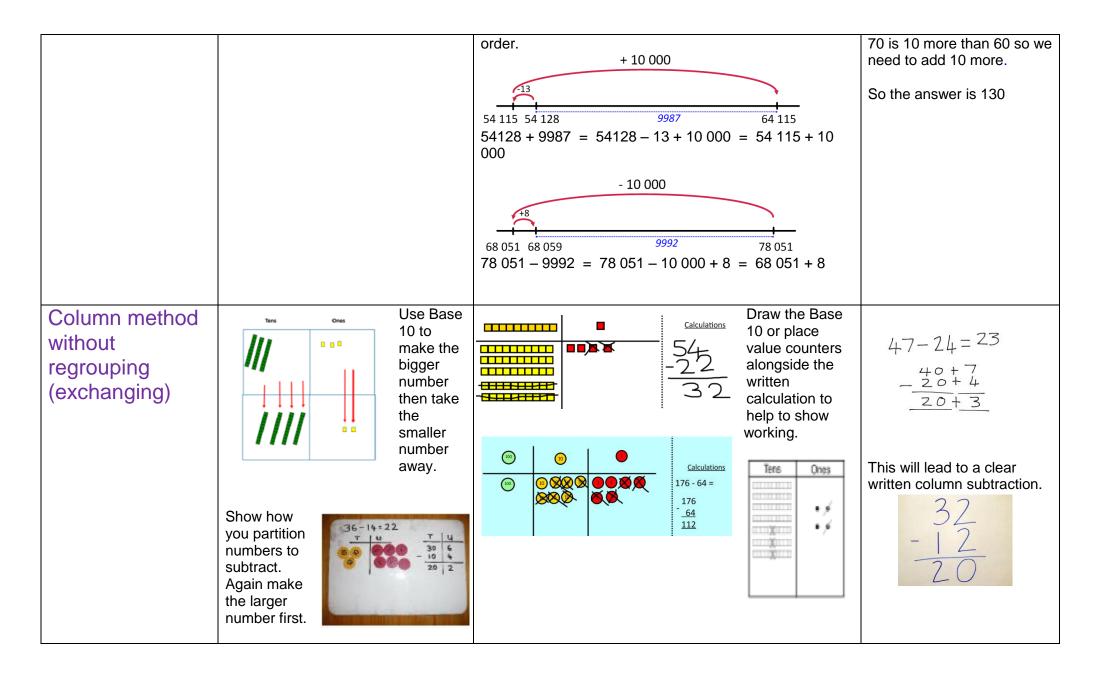


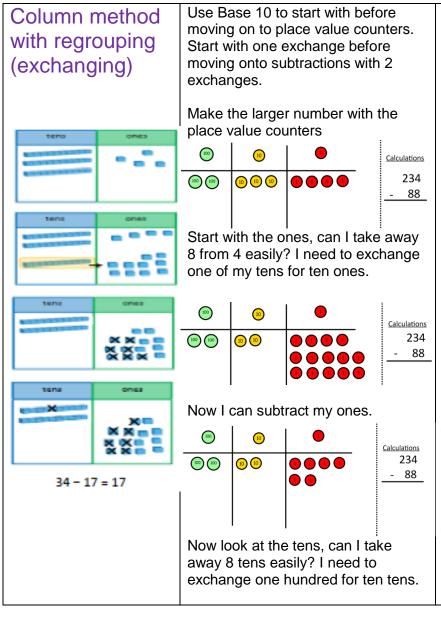
September 2017. Images and ideas drawn from Mathematics Mastery, White Rose Maths Hubs and various Camden schools' calculation policies.

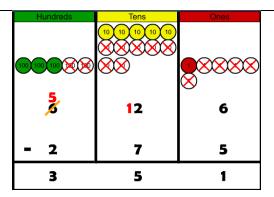
this method, beginning to identify when this method is more efficient than subtracting tens and then ones.			(we add because we took an extra 3 away when we subtracted 20 instead of 17).
Subtracting Multiples of Ten	Using the vocabulary of 1 ten, 2 tens, 3 tens etc. alongside 10, 20, 30 is important as pupils need to understand that it is a ten not a one that is being taken away. 40 = 60 - 20 38 - 10 = 28	5 tens - 2 tens = tens 50 - 20 =	32 – 10 = 22 Look at the number of tens in the largest number. Count back in tens to subtract the smaller number. 30, 20. Add on the number of ones that we originally had. = 22

Counting back in multiples of ten and one hundred.	Removing one group of 10 each time.	-10 -10 75 85 95 -100 -100 750 850 950	Counting back in 10s or 100s from any starting point. 53, 43, 33 540, 440, 340
Take away		Parts are place value amounts (canonical partitioning) - 300 - 4000 - 10 000 T5 421 Pupils should understand that the parts can be subtracted in any order. Parts are not place value amounts (non canonical partitioning) Make ten, make hundred, make thousand, make one - 9 000 - 5000 - 221 - 79 - 14 000 - 221 - 60 921 61 000 - 75 000 75 221	
Addition using compensation, rounding and adjustment		+ 10 000 54 128	Using near doubles. E.g. 70 + 60 = 60 + 60 - 120

September 2017. Images and ideas drawn from Mathematics Mastery, White Rose Maths Hubs and various Camden schools' calculation policies.



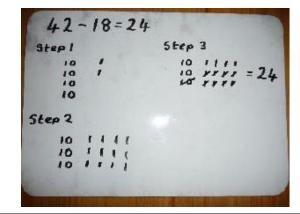


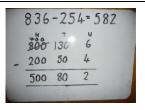


Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.

When confident, children can find their own way to record the exchange/regrouping.

Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup.



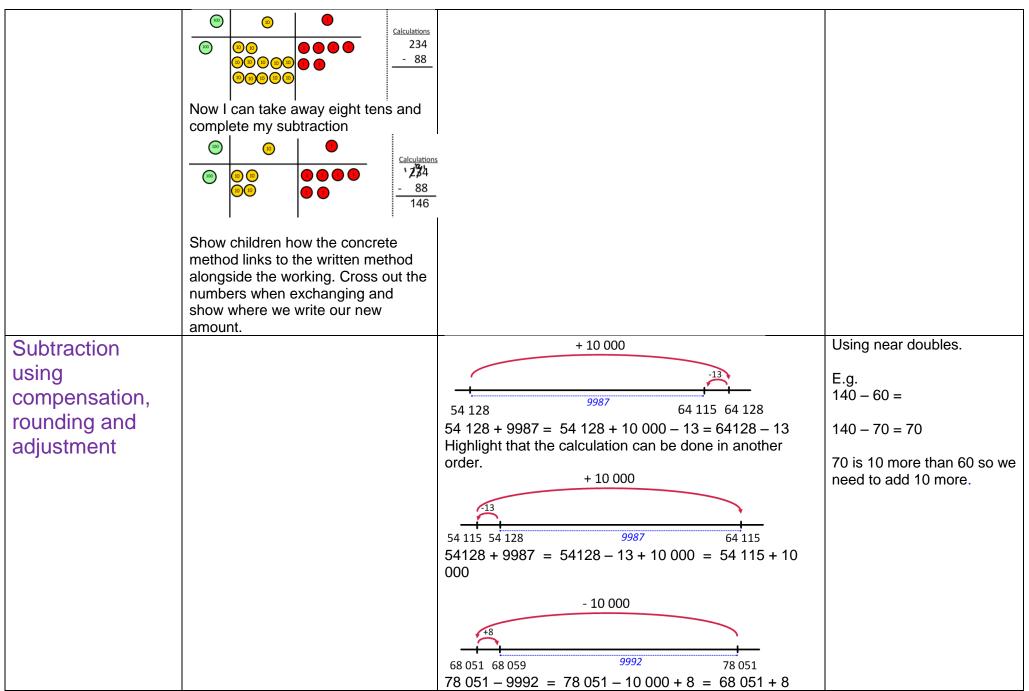


Children can start their formal written method by partitioning the number into clear place value columns.



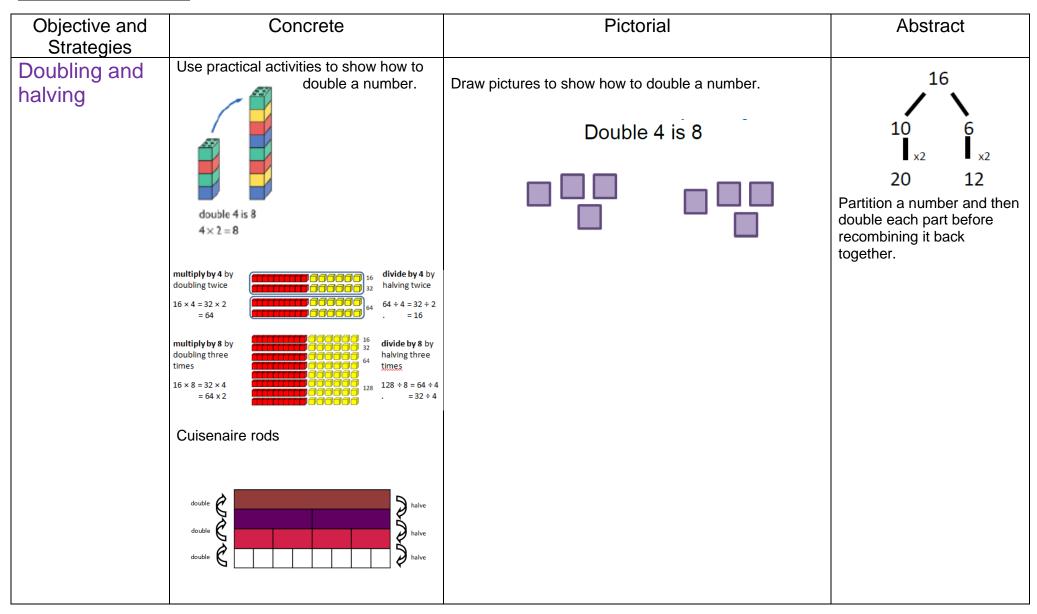
Moving forward the children use a more compact method.

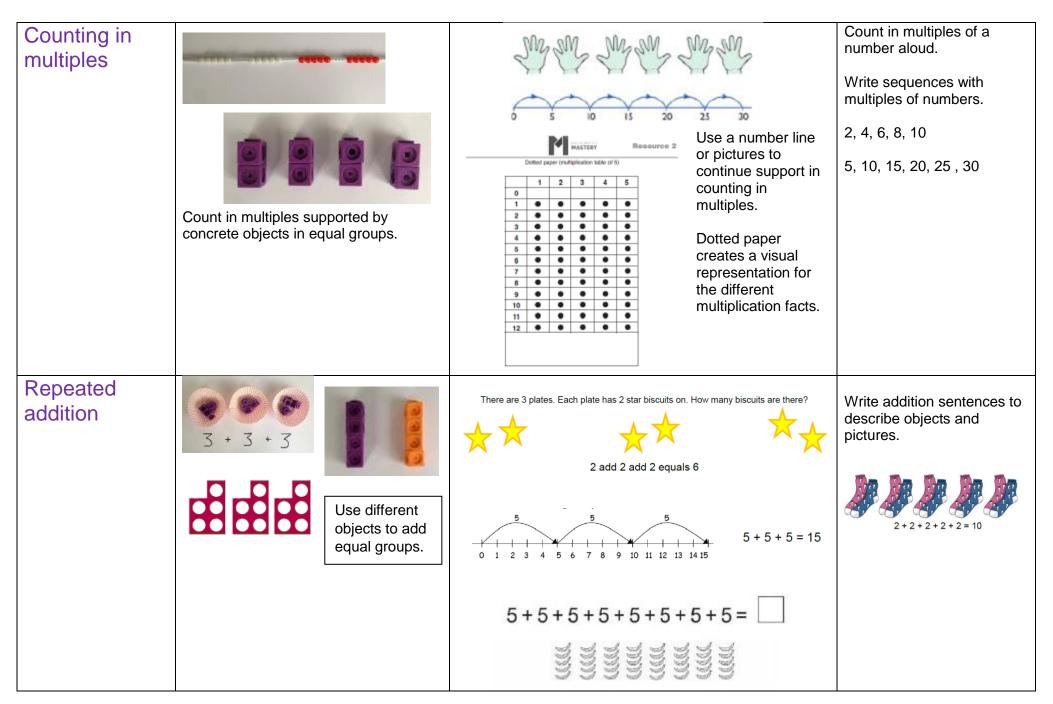
This will lead to an understanding of subtracting any number including decimals.



September 2017. Images and ideas drawn from Mathematics Mastery, White Rose Maths Hubs and various Camden schools' calculation policies.

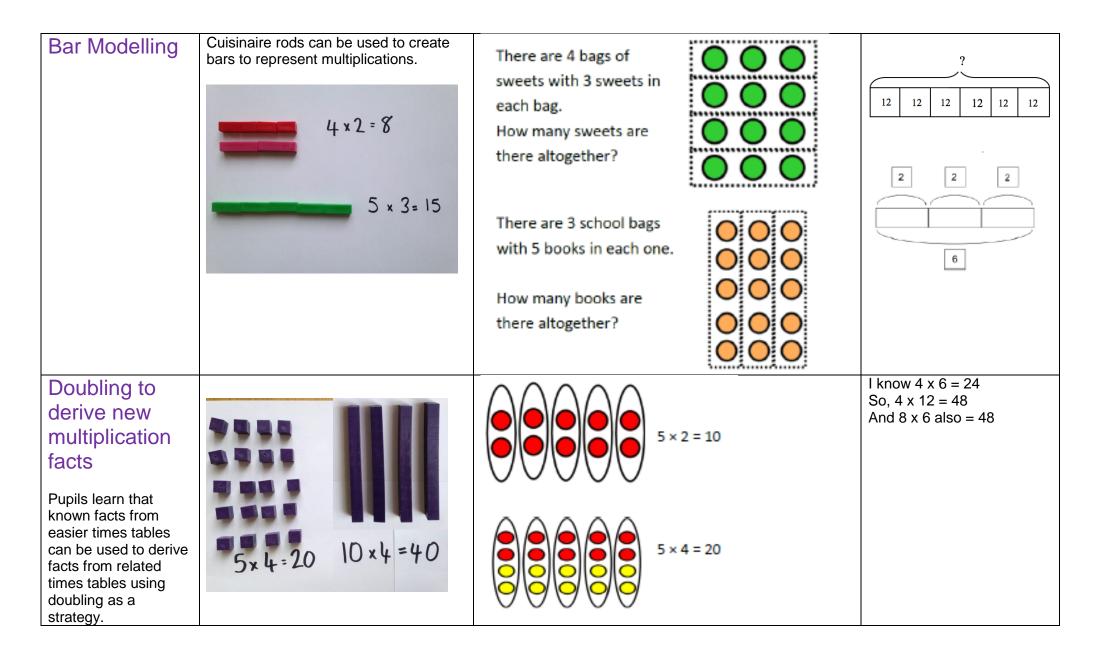
Multiplication





September 2017. Images and ideas drawn from Mathematics Mastery, White Rose Maths Hubs and various Camden schools' calculation policies.

Create arrays using counters/ cubes to Draw arrays in different rotations Use an array to write Arraysshow multiplication sentences. to find commutative multiplication sentences showing multiplication sentences. and reinforce repeated addition. commutative $2 \times 4 = 8$ multiplication 2 × 4 = 8 00000 00 00 ÖÖ 00000 $4 \times 2 = 8$ 5 + 5 + 5 = 15Link arrays to area of rectangles. 3 + 3 + 3 + 3 + 3 = 15 $5 \times 3 = 15$ $3 \times 5 = 15$ $12 = 3 \times 4$ 12 = 4 × 3

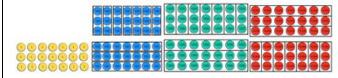


e.g. double 2x table to find 4 x table facts or double 6x5 to find 12x5 etc.

Applying the associative property allows pupils to see that this is the known fact multiplied by powers of ten. $7 \times 30 = 7 \times (3 \times 10) = (7 \times 3) \times 10$

2 100 000		700 000 x 3	70 000 x 30	7000 x 300	700 x 3000	70 x 30 000	7 x 300 000
210 000		70 000 x 3	7000 x 30	700 x 300	70 x 3000	7 x 30 000	
21 000		7000 x 3	700 x 30	70 x 300	7 x 3000		
2100		700 x 3	70 x 30	7 x 300		Ĩ	
210		70 x 3	7 x 30				
21	=	7 x 3		7			
2.1	Г	0.7 x 3	7 x 0.3	1			
0.21		0.07 x 3	0.7×0.3	7 x 0.03	7		

0.7 x 0.03



0.07 x 0.3

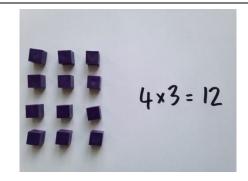
Inverse division facts can be derived:

0.021 0.007 x 3

$$6 \div 2 = 3$$
 $4 \times 3 = 12$
 $6 \div 3 = 2$
 $20 \times 3 = 60$
 $1/2 (4 \times 3) = 6 - 2 \times 3 = 6 - 200 \times 3 = 600$
 $2 \times 1_{1/2} = 3$
 $40 \times 3 = 120$
 $12 \times 3 = 10 \times 3 + 2 \times 3 = 30 + 6 = 36$

Ten times bigger

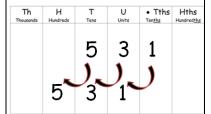
Pupils's work on this must be firmly based on concrete representations – the language of ten times bigger must be well modelled and understood to prevent the numerical misconception of 'adding 0'.



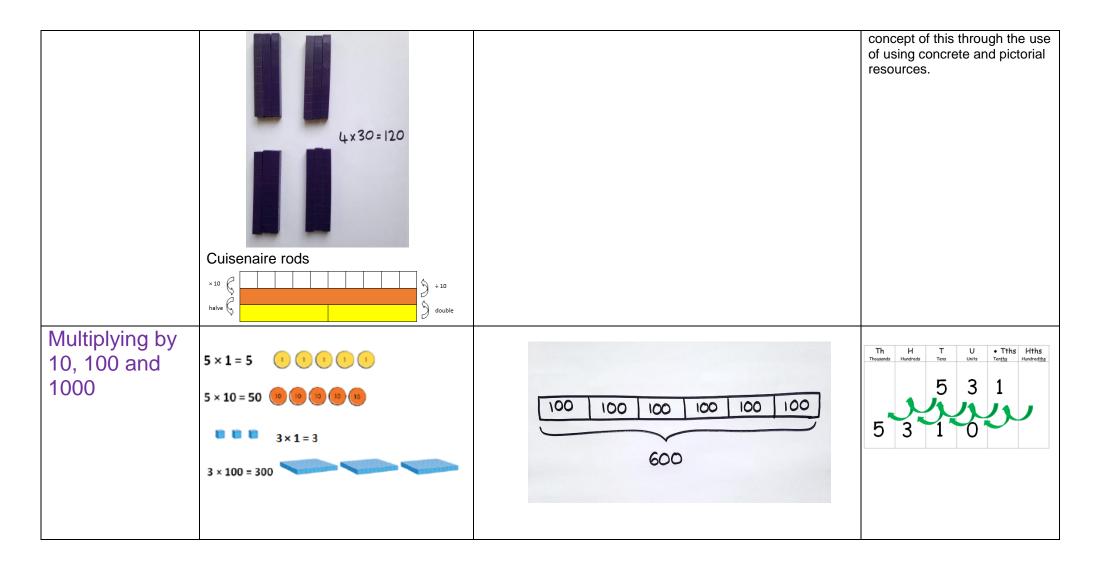




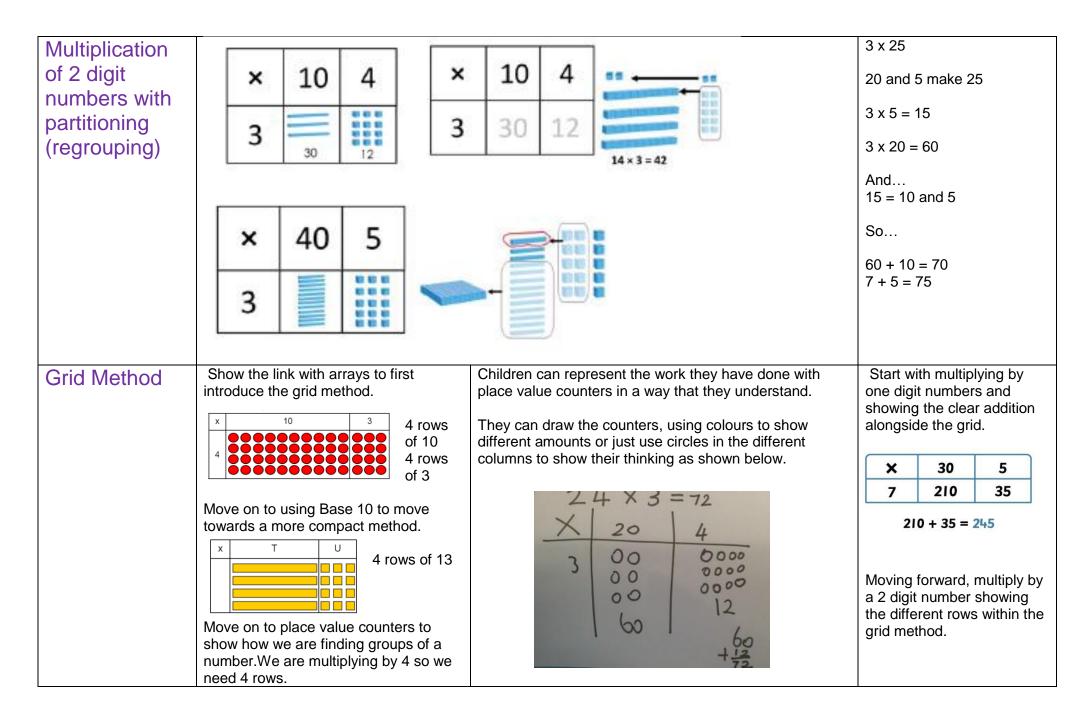
Possible misconcetion: move the deimal point.

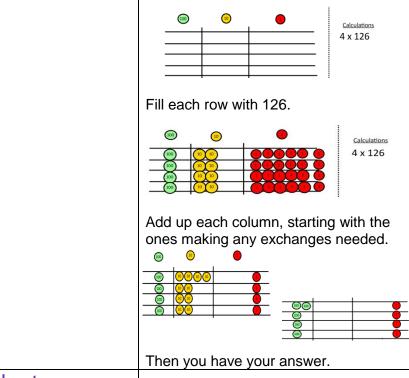


Encouarge children to keep the decimal point stationery and move the digits once to the left in order to make the number larger and the right to make the number smaller. This should only be used when the childrne understadn the



Distributive property	You can use dienes, counters etc. to illustrate this using arrays. Drawing out the boxes (see right) and building them up can be useful.	x 8 is 7 x 4 a 7 7 = 9 x 5 + 9	4	7 x 4: 7 x 8	1 1	2 x 8: 2 18 5 45
Multiplication of 2 digit numbers with partitioning (no regrouping)	3 x 12 12 = 10 + 2 3 X 10 3 X 2 Now add the total number of tens and ones.	x 3 ×	10	2 2 6		3 x 12 10 and 2 make 12 3 x 2 = 6 3 x 10 = 30 30 + 6 = 36
	Ondo.		3 x 12 =			

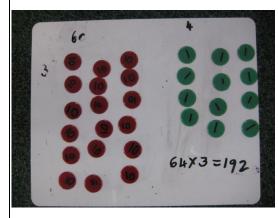




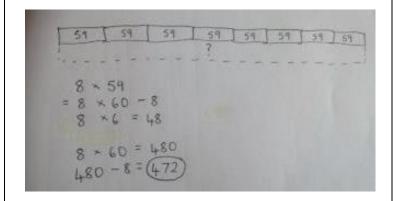
			8			
10	1		80			
3		30			24	
Х	1000	1000 300			2	
10	10000	10000 3000 40			20	
8	8000	8000 2400			16	

Short multiplication

It is important at this stage that children always multiply the ones first and note down their answer followed by the tens which they note below.

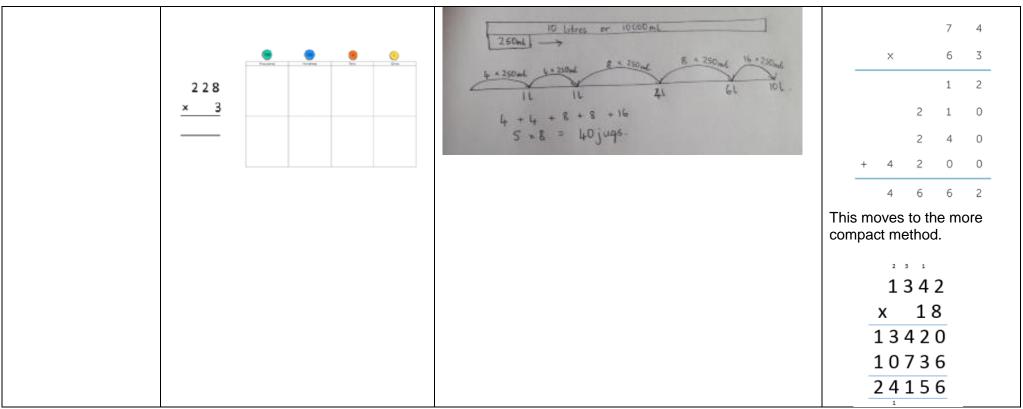


Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.



Start with long multiplication, reminding the children about lining up their numbers clearly in columns.

If it helps, children can write out what they are solving next to their answer.



National Curriculum appendix:

Long multiplication

24 × 16 becomes	124 × 26 becomes	124 × 26 becomes
2 2 4	1 2 1 2 4	1 2 1 2 4
× 1 6	× 2 6	× 2 6
2 4 0	2 4 8 0	7 4 4
1 4 4	7 4 4	2 4 8 0
3 8 4	3 2 2 4	3 2 2 4 1 1
Answer: 384	Answer: 3224	Answer: 3224

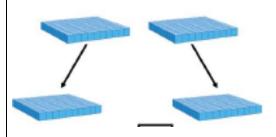
Note: Use a line in between the final factor and the answer for exhanging, rather than in the pictures to the left.

Division

Objective and Strategies	Concrete	Pictorial	Abstract
Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$	Share 9 buns between three people. $9 \div 3 = 3$
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	
		20 ? 20 ÷ 5 = ?	
	* * *	5 x ? = 20	

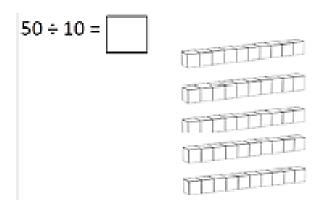
Dividing multiples of 10, 100 and 1000 by 10, 100 and 1000.

Pupils use the strategy of sharing into equal groups of tens, hundreds or thousands to reinforce their understanding of place value and the concept of division as sharing into equal groups. They master this skill with calculations where no partitioning is required, to prepare them for the next step



 $200 \div 100 = 2$

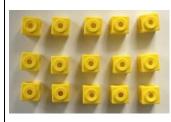
Here the child has selected the 100 dienes to use because they're dividing by 100. So 200 divided into groups of 100 = 2 groups.



 $6000 \div 200 = 30$

"I know there are five groups of 200 in 1000 and I have six 1000s and 5 x 6 = 30."

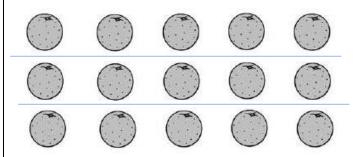
Division within arrays



Link division to multiplication by creating an array and thinking about the

number sentences that can be created.

Eg
$$15 \div 3 = 5$$
 $5 \times 3 = 15$
 $15 \div 5 = 3$ $3 \times 5 = 15$

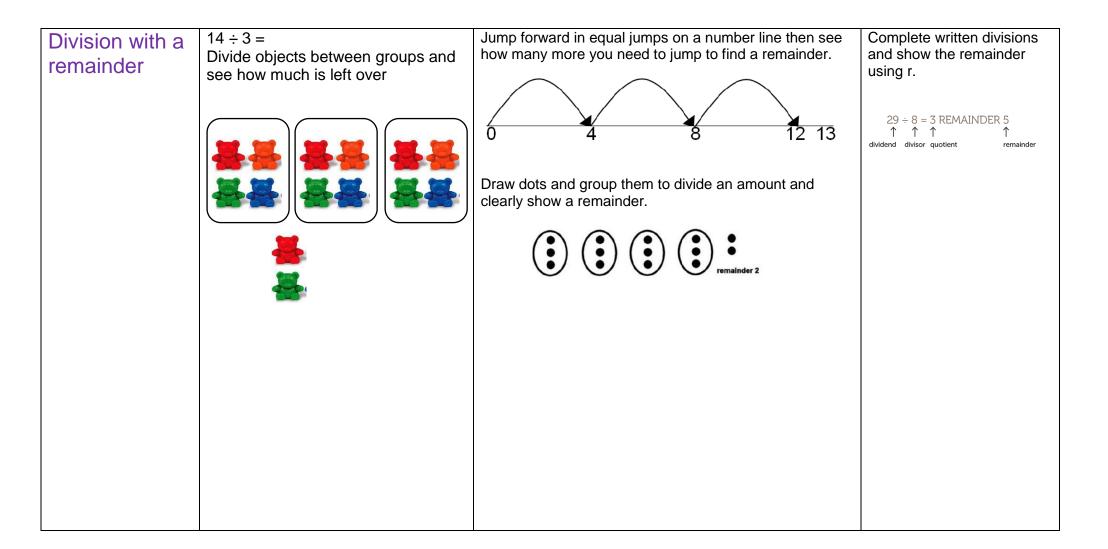


Draw an array and use lines to split the array into groups to make multiplication and division sentences.

Find the inverse of multiplication and division sentences by creating four linking number sentences.

$$7 \times 4 = 28$$

 $4 \times 7 = 28$
 $28 \div 7 = 4$
 $28 \div 4 = 7$



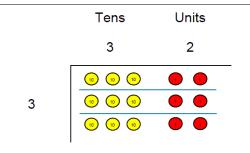
Short division

The difficulty with the short division algorithm comes with the confusion that can be caused by what you "think in your head" The thought process of the traditional algorithm is as follows:

How many 4s in 8? 2

How many 4s in 5? 1 with 1 remaining so regroup. How many 4s in 12? 3 How many 4s in 8? 2 Warning: If you simply apply place value knowledge to each step, the thinking goes wrong if you have to regroup. How many 4s in 500? 100 with 1 remaining (illogical) The answer would be 125 Sharing the dividend builds conceptual understanding however doesn't scaffold the "thinking" of the algorithm.

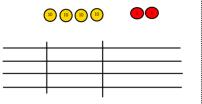
Using place value counters and finding groups of the divisor for each power of ten will build conceptual understanding of the compact short division algorithm.



Use place value counters to divide using the bus stop method alongside

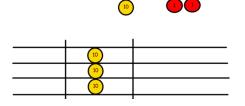
Calculations

42 ÷ 3

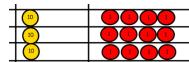


 $42 \div 3 =$

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.

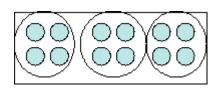


We exchange this ten for ten ones and then share the ones equally among the groups.



We look how much there is in 1 group; the answer is 14.

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



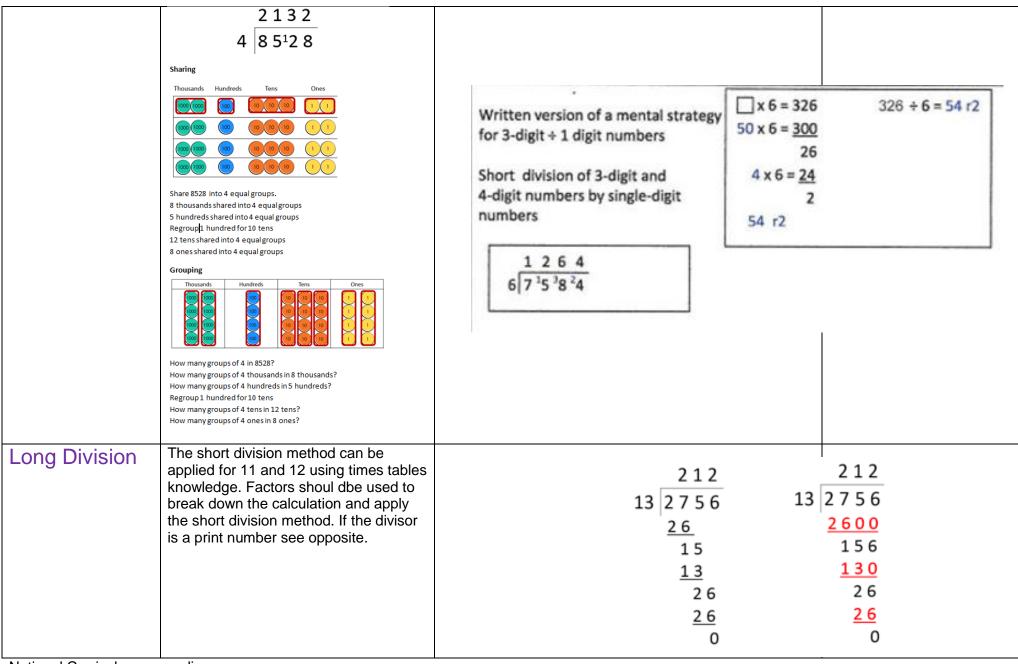
Encourage them to move towards counting in multiples to divide more efficiently.

Begin with divisions that divide equally.

Move onto divisions with a remainder.

Finally move into decimal places to divide the total accurately.

See below for written strategies:



National Curriculum appendix:

September 2017. Images and ideas drawn from Mathematics Mastery, White Rose Maths Hubs and various Camden schools' calculation policies.

Short division

98 ÷ 7 becomes

Answer: 14

432 ÷ 5 becomes

Answer: 86 remainder 2

496 ÷ 11 becomes

Answer: $45\frac{1}{11}$

Long division

432 ÷ 15 becomes

432 ÷ 15 becomes

432 ÷ 15 becomes